


# Force - Field - Energy - Potential

	<p>Force</p>	<p>Field</p>	<p><math>E_{pot}</math>  <math>W_g = -\Delta E_{pot}</math></p> <p><small><math>W_g</math>: Work by field</small></p>	<p>Potential  <math>\frac{W_g}{test} = -\Delta V</math></p>	<p>Increment of potential</p>	<p>Homogeneous case</p>
<p>Ed</p>	<p><math>F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}</math>  <math>[N]</math></p> <p>Vector-form:  <math>\vec{F}_{21} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \frac{\vec{r}}{r}</math>  <small>(Force on 2 from 1)</small></p>	<p><math>E = \frac{F}{q_2}</math>  <math>[\frac{N}{C} = \frac{V}{m}]</math></p> <p>Vector</p> <p><small>(Field-source: 1)          Test-charge: <math>q_2</math>)</small></p>	<p><math>E_{pot} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}</math>  <math>[J]</math> scalar</p> <p><small><math>E_{pot}</math> = work of field to move object from <math>r</math> to where <math>E_{pot} = 0</math>.  <math>F = -\frac{\Delta E_{pot}}{\Delta x}</math>          Small <math>\Delta x</math></small></p>	<p><math>V = \frac{E_{pot}}{q_2}</math>  <math>[\frac{J}{C} = V]</math></p> <p><math>W_g = -q_2 \Delta V</math></p> <p><small><math>E = -\frac{\Delta V}{\Delta x}</math>          Small <math>\Delta x</math></small></p>	<p><math>\Delta V = \frac{\Delta E_{pot}}{q_2}</math>  <math>W_g = -\Delta E_{pot} = -q_2 \Delta V</math></p>	<p>Homogeneous:    <math>V_a</math> Capacitor  <math>\Delta V = V_b - V_a = V</math>  <math>E = \frac{\Delta V}{\Delta x} \cdot  \vec{E}  = \frac{V}{d}</math></p> <p>Normalized:  <math>E = \frac{V}{d}</math>  <small>(<math>Q = CV</math>, <math>C = \epsilon_0 \frac{A}{d}</math>)  <math>(E = \frac{Q}{\epsilon_0 d})</math></small></p>
<p>Grav.</p>	<p><math>F = G \frac{m_1 m_2}{r^2}</math>  <math>[N]</math></p> <p>Vector-form:  <math>\vec{F}_{21} = -G \frac{m_1 m_2}{r^2} \frac{\vec{r}}{r}</math>  <small>(Force on 2 from 1)</small></p>	<p><math>g_f = \frac{F}{m_2}</math>  <math>[\frac{N}{kg} = \frac{m}{s^2}]</math></p> <p>Vector</p> <p><small>(Field-source: 1          Test-mass: <math>m_2</math>)</small></p>	<p><math>E_{pot} = -G \frac{m_1 m_2}{r}</math>  <math>[J]</math> scalar</p> <p><small><math>F = -\frac{\Delta E_{pot}}{\Delta x}</math>          Small <math>\Delta x</math></small></p>	<p><math>V = \frac{E_{pot}}{m_2}</math>  <math>[\frac{J}{kg} = \frac{m^2}{s^2}]</math></p> <p><math>W_g = -m_2 \Delta V</math></p> <p><small><math>E = -\frac{\Delta V}{\Delta x}</math>          Small <math>\Delta x</math></small></p>	<p><math>\Delta V = \frac{\Delta E_{pot}}{m_2}</math>  <math>W_g = -\Delta E_{pot} = -m_2 \Delta V</math></p>	<p>Near Earth-surface:  <math>F = -mg</math>  <small>(and same direction)</small>  <math>E_{pot} = mgh</math></p> <p>Normalized:  <math>F = \frac{E_{pot}}{h}</math>  <math>g = \frac{V}{h}</math></p>

Remember:  $W = \Delta E_{kin} = -\Delta E_{pot}$  if mech. energy conserved.

Homogeneous case of ed:  $\Delta E_{kin} = -\Delta E_{pot} = -q_2 \Delta V = q_2 \cdot E \cdot \Delta x$  even for large  $\Delta x$